

# Modelling viscosity of TiO<sub>x</sub> containing silicate melts

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Experimental studies on viscosity of titanium bearing slags have been reviewed and the assessed data were used in extending the capability of the structurally related viscosity model for silicate melts, developed by the present authors. Experimental data on ternary and higher order systems containing CaO, MgO, MnO, FeO, Al<sub>2</sub>O<sub>3</sub>, TiO<sub>2</sub>, Ti<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub> were assessed and used. The newly extended viscosity model represented the viscosity behaviour over broad temperature and composition ranges. The structural role played by TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> in silicate network structure is discussed with respect to their effect on viscosity of melts.

Keywords: viscosity model, TiO<sub>x</sub> containing silicate melts, silicate network structure.

## Introduction

Titaniferous ore is sometimes used as a feed material for production of hot metal in electric arc and blast furnaces. The reducing conditions in these furnaces result in low FeO slags containing up to 35% TiO<sub>x</sub> in a matrix of Al<sub>2</sub>O<sub>3</sub>-CaO-SiO<sub>2</sub>-MgO-MnO. For improved operation of these ironmaking processes, modifications to the slags' chemistry could result in reducing the liquidus temperature and viscosity of the slag produced.

Previous studies by Holmes *et al.*<sup>1</sup> and Ratchev and Belton<sup>2</sup> have established the effects of slag chemistry and oxidation state on the liquidus region of titania rich slags. It was found that reduction of TiO<sub>2</sub> to Ti<sub>2</sub>O<sub>3</sub> can have a pronounced effect on the liquidus temperature of such slags<sup>2</sup>. Similarly, there are published data on the viscosity of ternary and higher order systems containing varying concentrations of titanium oxides<sup>3-14</sup>. The influence of TiO<sub>2</sub> to Ti<sub>2</sub>O<sub>3</sub> on viscosity of silicate slag has been studied in both homogeneous liquid and melts containing solid particles. It was found that for a given slag, additions of TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> caused viscosity to decrease at a given temperature above the liquidus. However, the presence of the solid phase at temperatures below the liquidus resulted in a sharp rise in the viscosity.

It should be mentioned that the effect of a particular oxide component on viscosity should be considered in two aspects. The first is the effect on the homogeneous liquid, for example in silicate melts, additions of so called network modifiers, such as CaO and MnO, will in general reduce viscosity. Such an effect may be related to the bonding characteristic of the oxides concerned, as discussed previously by the present authors<sup>15-17</sup>.

The second effect comes from the influence of the oxides on the liquidus temperature of the melts. If the addition of a certain amount of a particular oxide stabilizes a solid phase, the viscosity of the melt is expected to rise sharply with an increasing amount of the solid phases. The latter effect can very often override the effect on the homogeneous liquid phase.

The present work was part of ongoing development of a multi-phase reaction model at CSIRO<sup>18</sup>. The package enables metallurgists to simulate reactions in

pyrometallurgical processes with respect to equilibrium between various phases, and to calculate slag viscosity at elevated temperatures. The viscosity model developed by the present authors during the past decade relates viscosity to the structural properties of the silicate melts<sup>15-17</sup>. The classification of oxide components as glass former, modifier and amphoteric as proposed by Urbain<sup>21</sup> was adopted to distinguish the structural role played by various oxides and analyse their contributions to viscosity. Such an approach has made it possible to describe viscosity behaviour of high order systems using binary model parameters only. The model has been validated using published data from binary to multi-component systems (silicate and calcium ferrite type), as well as various types of industrial slags<sup>15-20</sup>. The oxide components included in the model currently, are SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, Fe<sub>2</sub>O<sub>3</sub>, TiO<sub>2</sub>, Ti<sub>2</sub>O<sub>3</sub>, CaO, MgO, MnO, FeO, PbO, NiO, Cu<sub>2</sub>O, ZnO and CoO. Details of the formulation of the model and most of the validation results can be found elsewhere<sup>15-20</sup>.

In the present paper, application of the current modelling approach to multi-component silicate slags containing TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> will be discussed. The extension of our viscosity model to TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> containing silicate melts was based on analysis and review of the experimental data.

## Review of viscosity data

### CaO-TiO<sub>2</sub>-SiO<sub>2</sub> system

A number of groups<sup>3,9-14</sup> have measured the viscosity in the CaO-TiO<sub>2</sub>-SiO<sub>2</sub> system and have shown that addition of TiO<sub>2</sub> reduces the viscosity of CaO-SiO<sub>2</sub> based melts. However, there is a large scatter among different studies and it was found that the data by Dingwell<sup>9</sup> are most accurate. Dingwell's measurements were carried out under well controlled conditions, i.e., in air and using Pt-20%Rh components. Under such conditions the slags can be considered free of Ti<sub>2</sub>O<sub>3</sub> and other contaminants. Furthermore, only data in the liquid region were reported, which covered the targeted composition range of 10 to 80 mol% TiO<sub>2</sub> along the CaSiO<sub>3</sub>-TiO<sub>2</sub> join, and the temperature range of 1400-1600°C. Figure 1 presents Dingwell's data, where the effect TiO<sub>2</sub> additions to the

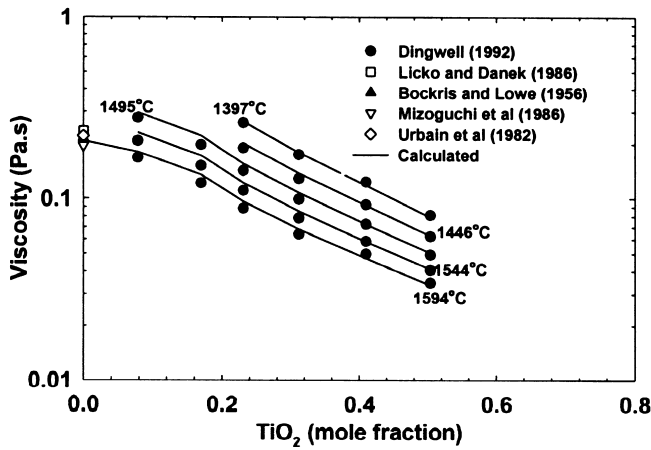


Figure 1. Comparison between the calculated viscosity and the experimental data<sup>9</sup> on the effect of TiO<sub>2</sub> addition along the CaSiO<sub>3</sub>-TiO<sub>2</sub> join in the CaO-TiO<sub>2</sub>-SiO<sub>2</sub> system

CaO-SiO<sub>2</sub> binary melt, with unit molar ratio CaO/SiO<sub>2</sub>, is shown at different temperatures. It is apparent that at a given temperature, addition of TiO<sub>2</sub> causes viscosity to decrease. It is also noted that the measured viscosity for the CaO-SiO<sub>2</sub> binary melt at 1600°C by Dingwell agree well with other published data<sup>22-25</sup> (Figure 1).

It should be mentioned that the compositions reported by Dingwell<sup>9</sup>, which were obtained after the viscosity measurements, were used for the construction of Figure 1. These compositions for TiO<sub>2</sub> were generally lower than the targeted values and were not available for TiO<sub>2</sub> greater than 50 mol%. Furthermore, CaO/SiO<sub>2</sub> ratios were in a range of 0.94–0.98, rather than unity as targeted.

#### MnO-TiO<sub>2</sub>-SiO<sub>2</sub> system

Viscosity behaviour in the MnO-TiO<sub>2</sub>-SiO<sub>2</sub> system was investigated by Yagi *et al.*<sup>13</sup> over a temperature range of 1400–1600°C with silica mole fractions varying from 0 to 0.5. Pt-Rh alloy components were used for these measurements, thus avoiding contamination of the melts. Figure 2 shows their results on the effect of substituting TiO<sub>2</sub> for MnO at given silica mole fractions at 1600°C.

It is evident that for a given silica content (mole fraction), substitution of TiO<sub>2</sub> for MnO does not seem to cause significant change in the viscosity of these slags. This implies that TiO<sub>2</sub> and MnO have very similar effects on the viscosity of silicate melts.

#### MgO-TiO<sub>2</sub>-SiO<sub>2</sub> system

In this ternary system only two experimental datum points by Nakamura *et al.*<sup>11</sup> were found. These measurements were on a 35%(mol)MgO-30%SiO<sub>2</sub>-35% TiO<sub>2</sub> slag at 1500 and 1550 C. The results showed a viscosity decrease of 0.011 Pa.s as the temperature was increased from 1500 to 1550°C.

#### PbO-TiO<sub>2</sub>-SiO<sub>2</sub> system

Nakamura *et al.* also investigated the effect of the addition of TiO<sub>2</sub> to the PbO-SiO<sub>2</sub> binary melts on viscosity<sup>11</sup>. Their study covered a temperature range of 800–1300°C and TiO<sub>2</sub> content of 0 to 0.3 mole fraction at PbO/SiO<sub>2</sub> mole ratio of 1, 3/2 and 7/3. Their data showed that at the mole ratio of PbO/SiO<sub>2</sub> =1, TiO<sub>2</sub> addition resulted in a decrease in viscosity, while when PbO/SiO<sub>2</sub> =7/3, addition of TiO<sub>2</sub> had an opposite effect. Figure 3 shows the data at 1150°C, for which more datum points are available.

#### CaO-Al<sub>2</sub>O<sub>3</sub>-TiO<sub>2</sub>-SiO<sub>2</sub> system

Ohno and Ross<sup>3</sup> studied viscosity in the CaO-TiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> system. Their measurements covered composition range of CaO/SiO<sub>2</sub> ratio=0.6, 1.0 and 1.16 and TiO<sub>2</sub> contents of 0 to 45 wt% between 1400–1500°C. The Al<sub>2</sub>O<sub>3</sub> levels were fixed at 10 and 20 wt%. Froberg and Weber<sup>14</sup> also reported viscosity data in this quaternary system, with Al<sub>2</sub>O<sub>3</sub> levels of 0 to 20 wt% (with 5 wt% interval) at 1600°C. Both sets of data showed that at a given temperature and CaO/SiO<sub>2</sub> ratio, viscosity decreased with TiO<sub>2</sub> addition. Figure 4 presents the data by Ohno and Ross<sup>3</sup> measured at 1500°C. It can be seen that viscosity decreased as TiO<sub>2</sub> addition increased at a given CaO/SiO<sub>2</sub> ratio. It also showed that the higher level of Al<sub>2</sub>O<sub>3</sub> corresponded to higher values of viscosity.

#### Blast furnace type slags

Measurements on blast furnace type slags containing CaO, MgO, TiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub> and SiO<sub>2</sub> under neutral atmospheres have been reported by Xie *et al.*<sup>4</sup> and Van der Colf and Howat<sup>5</sup>. The composition and temperature ranges covered by the two studies are listed in Table I. Both sets of data covered similar composition range. Handfield *et al.* have

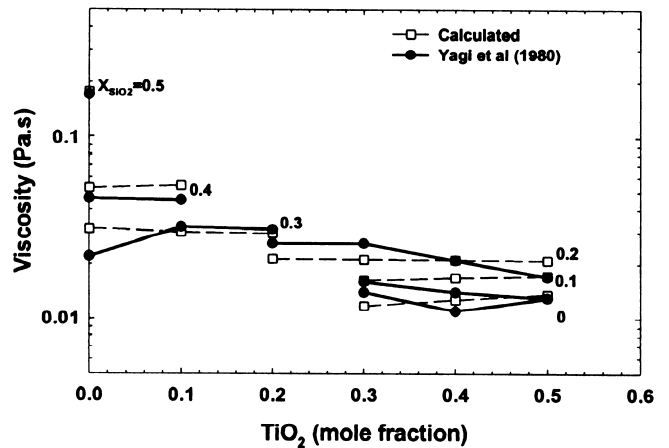


Figure 2. Comparison between the calculated viscosity and the experimental data<sup>13</sup> on the effect of substitution of TiO<sub>2</sub> for MnO in the MnO-TiO<sub>2</sub>-SiO<sub>2</sub> system at 1600°C

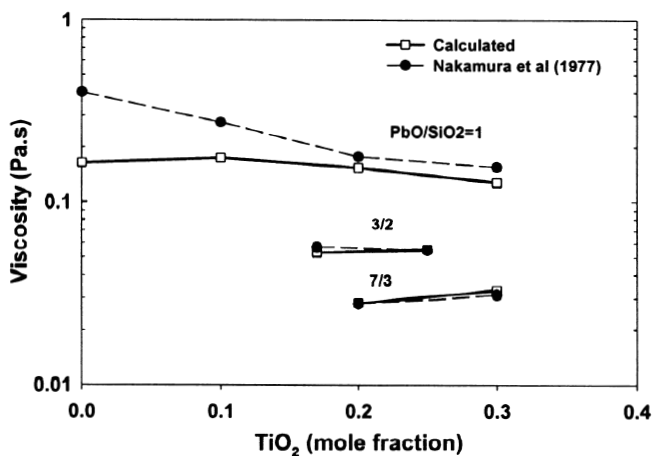


Figure 3. Comparison between the calculated viscosity and the experimental data<sup>11</sup> on the effect of addition of TiO<sub>2</sub> to the PbO-TiO<sub>2</sub>-SiO<sub>2</sub> system at 115°C

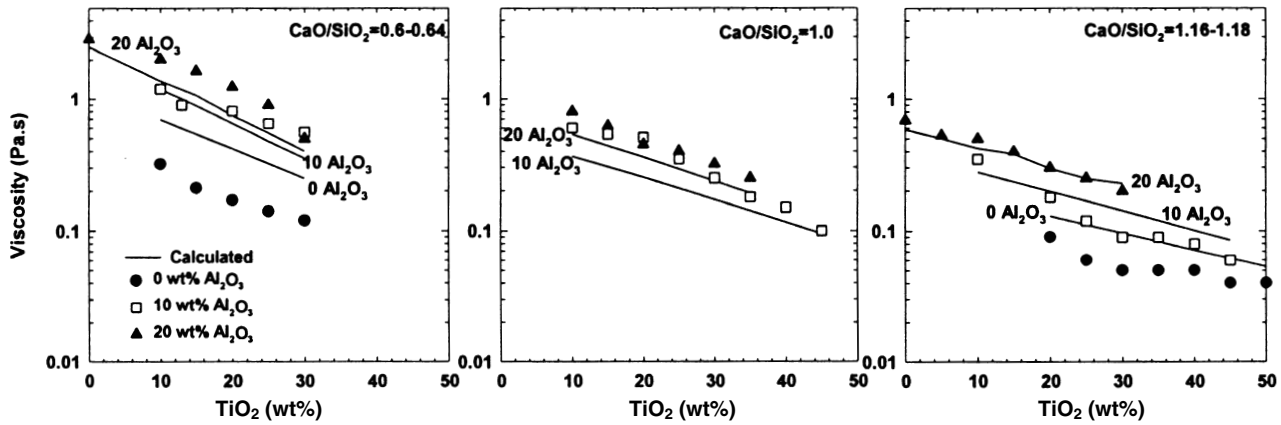


Figure 4. Comparison between the calculated viscosity and the experimental data at 1500°C<sup>3</sup> in the CaO- Al<sub>2</sub>O<sub>3</sub>-TiO<sub>2</sub>-SiO<sub>2</sub> system

Table I  
Experimental conditions used in the viscosity measurements by Xie *et al.*<sup>4</sup> and Van der Colf and Howat<sup>5</sup>

Ref	T (°C)	Composition wt%				
		SiO <sub>2</sub>	TiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	CaO	MgO
[4]	1240–1540	21–29	17–33	9–19	24–31	7–16
[5]	1322–1492	21–31	25–30.2	11.2–13.8	8.3–24	8.3–23.5

investigated the influence of TiO<sub>2</sub>, TiO and Ti<sub>2</sub>O<sub>3</sub> additions and temperature (~1300–1600°C) on a blast furnace type slag from the Steel Company of Canada in both homogeneous liquid and melts containing solid particles<sup>6-7</sup>. The slag contained 37% SiO<sub>2</sub>, 35 wt% CaO, 18% MgO, 1.2% TiO<sub>2</sub>, 4% Al<sub>2</sub>O<sub>3</sub>, 1.2% S, 0.4% MnO, 0.2% Fe and 1.3% others. Molybdenum components were used in the viscosity measurements.

These measurements found that at a given temperature, addition of TiO<sub>2</sub> or Ti<sub>2</sub>O<sub>3</sub> reduces the viscosity of the blast furnace type slags, for example the data by Xie *et al.*<sup>4</sup> and Van der Colf and Howat<sup>5</sup> as shown in Figure 5, and results by Handfield *et al.*<sup>6-7</sup> in Figures 6 and 7. It should be mentioned that only data in fully liquid region were shown in order to make comparison with the model. Three samples each with similar chemistry were chosen and shown in Figure 5. It is noted that the data by Van der Colf and Howat<sup>5</sup> are consistently lower than those by Xie *et al.*<sup>4</sup> though slag chemistry of samples chosen were close to each other.

### Modelling results

As mentioned above, one of the objectives of the present work was to extend the capability of CSIRO's structurally related viscosity model for multi-component silicate melts to TiO<sub>x</sub> containing slags. This model predicts viscosity of higher order systems using only binary parameters. For example, viscosity of the CaO-TiO<sub>2</sub>-SiO<sub>2</sub> system can be predicted by using parameters determined for the two CaO-SiO<sub>2</sub> and TiO<sub>2</sub>-SiO<sub>2</sub> binaries. Details of the formulation of the model and most of the validation results can be found in elsewhere<sup>15-17</sup>.

Due to the lack of viscosity data for the binary TiO<sub>2</sub>-SiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> systems, data on the CaO-TiO<sub>2</sub>-SiO<sub>2</sub> ternary by Dingwell<sup>9</sup> were used in determination of the model parameters for the TiO<sub>2</sub>-SiO<sub>2</sub> binary. The viscosity data of the CaO-TiO<sub>2</sub>-SiO<sub>2</sub><sup>9</sup> and MnO-TiO<sub>2</sub>-SiO<sub>2</sub><sup>13</sup> systems

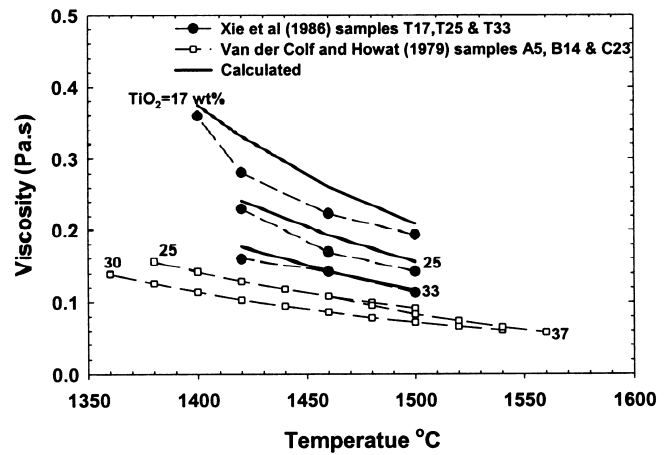


Figure 5. Comparison between the calculated viscosity and the experimental data<sup>4,5</sup> on the effect of TiO<sub>2</sub> addition to multi-component blast furnace type slags

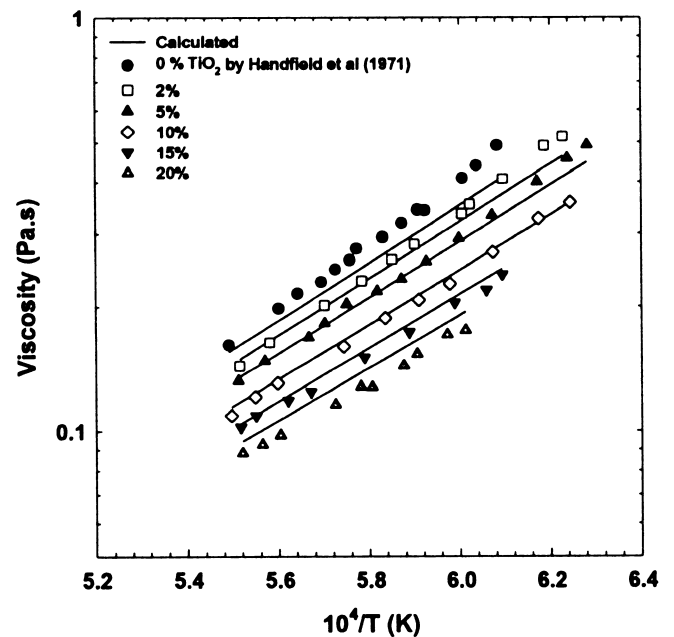


Figure 6. Comparison between the calculated viscosity and the experimental data by Handfield *et al.*<sup>6</sup> on the effect of TiO<sub>2</sub> addition to multi-component blast furnace type slags

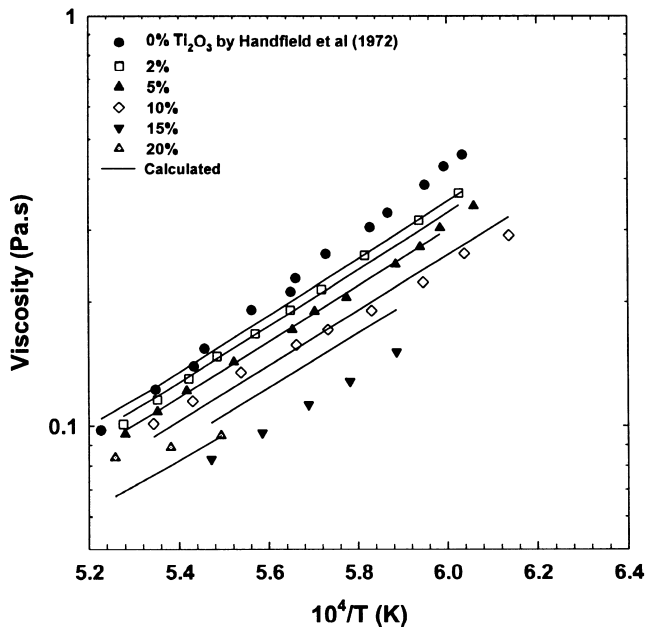


Figure 7. Comparison between the calculated viscosity and the experimental data by Handfield *et al.*<sup>7</sup> on the effect of  $\text{Ti}_2\text{O}_3$  addition to multi-component blast furnace type slags

revealed that  $\text{TiO}_2$  affects the viscosity in a similar manner to metal oxides, such as  $\text{CaO}$  and  $\text{MnO}$ , over a silica content of 0 to 0.5 mole fraction and  $\text{TiO}_2$  up to 0.8. Based on this behaviour,  $\text{TiO}_2$  and  $\text{Ti}_2\text{O}_3$  were treated as network modifiers in the model. The model parameters for the  $\text{TiO}_2$ - $\text{SiO}_2$  binary were used for the  $\text{Ti}_2\text{O}_3$ - $\text{SiO}_2$  binary and  $\text{TiO}_{1.5}$  was used as an oxide component in the model the same way as  $\text{Fe}_2\text{O}_3$  was treated in the model<sup>16</sup>.

It should be mentioned that the following comparison between modelling results and the experimental data covers only the data in homogeneous liquid region. This is because the purpose of the present paper is to validate the liquid viscosity model, though the multi-phase reaction model mentioned earlier is able to produce estimated viscosity values for solid containing melts, which combines viscosity models with the thermodynamic models to calculate equilibrium among phases<sup>18</sup>.

### Ternary systems

Figures 1 and 2 show a comparison between the calculated viscosity and the experimental data in the  $\text{CaO}$ - $\text{TiO}_2$ - $\text{SiO}_2$  and  $\text{MnO}$ - $\text{TiO}_2$ - $\text{SiO}_2$  systems. Excellent agreement between the calculated viscosity and the experimental data were obtained. Figure 3 shows the agreement between the model prediction and the measurements to be close, except two compositions, i.e., at 0 and 10%  $\text{TiO}_2$  additions and  $\text{PbO}/\text{SiO}_2 = 1$ . The calculated viscosity for  $\text{TiO}_2$  free binary  $\text{PbO}$ - $\text{SiO}_2$  is lower than the measured value.

The model parameters for the binary system were determined by fitting data of the  $\text{PbO}$ - $\text{SiO}_2$  system, which were measured in the temperature range of 800–1000°C<sup>19</sup>. The difference suggests the model may require refinement at higher temperatures. The experimental data showed that viscosity decreased continuously with  $\text{TiO}_2$  addition at  $\text{PbO}/\text{SiO}_2 = 1$ . However, the model predicted that initial addition of  $\text{TiO}_2$  to the binary would cause viscosity to increase slightly, while further additions led to a reduction in viscosity. This can be explained as follows. When  $\text{TiO}_2$  was added to the binary melts, there are two effects

occurring. One is the dilution of  $\text{SiO}_2$ ; the other is that  $\text{PbO}$  is expected to reduce viscosity more effectively than  $\text{TiO}_2$  at a given  $\text{SiO}_2$  mole fraction and temperature. Such an effect has been discussed previously by the present authors regarding the relative stability of oxide components<sup>15–17</sup>. In other words at a given  $\text{SiO}_2$  mole fraction, substitution of  $\text{TiO}_2$  for  $\text{PbO}$  is expected to result in a slight increase in viscosity. The model calculation showed the decrease in viscosity caused by  $\text{SiO}_2$  dilution to be as effective as the tendency of  $\text{TiO}_2$  to increase viscosity at 0.1 mole fraction  $\text{TiO}_2$ . However, the dilution effect dominates with further addition of  $\text{TiO}_2$ .

### $\text{CaO}$ - $\text{Al}_2\text{O}_3$ - $\text{TiO}_2$ - $\text{SiO}_2$ system

Comparison between the calculated viscosity and the experimental data by Ohno and Ross<sup>3</sup> and Froberg and Weber<sup>14</sup> in the  $\text{CaO}$ - $\text{Al}_2\text{O}_3$ - $\text{TiO}_2$ - $\text{SiO}_2$  system was carried out. It was found that the fit to the data by Ohno and Ross was within  $\pm 50\%$  uncertainty. However, there are large discrepancies between calculated values and the data by Froberg and Weber<sup>14</sup>. The data by Froberg and Weber<sup>14</sup> are systematically higher than model predictions. Due to limited space, only the comparison of modelling results with data by Ohno and Ross<sup>3</sup> at 1500°C were presented in Figure 4. It can be seen that the model can represent the correct trend in regard to the effects of  $\text{CaO}/\text{SiO}_2$  (wt%/wt%) ratio,  $\text{Al}_2\text{O}_3$  level and  $\text{TiO}_2$  additions on viscosity. The fit to the data in most cases is within 30% uncertainty. The poor fit to the data at 0 wt%  $\text{Al}_2\text{O}_3$  implies disagreement between the data by Dingwell<sup>9</sup> and those by Ohno and Ross<sup>3</sup> for the ternary  $\text{CaO}$ - $\text{TiO}_2$ - $\text{SiO}_2$  system.

### Blast furnace type slags

The current viscosity model was used to predict viscosity of the blast furnace type slags. For convenience, the initial composition used in the model for the slags of Handfield *et al.*<sup>6–7</sup> was 37%  $\text{SiO}_2$ , 35wt %  $\text{CaO}$ , 18%  $\text{MgO}$ , 1.2%  $\text{TiO}_2$ , 4%  $\text{Al}_2\text{O}_3$ , and 4.8%  $\text{FeO}$ . The minor components, such as S,  $\text{MnO}$  and others were added in  $\text{FeO}$ . The overall fit of the predicted viscosity values to the measured data<sup>4–8</sup> for blast furnace type slag is shown in Figure 8.

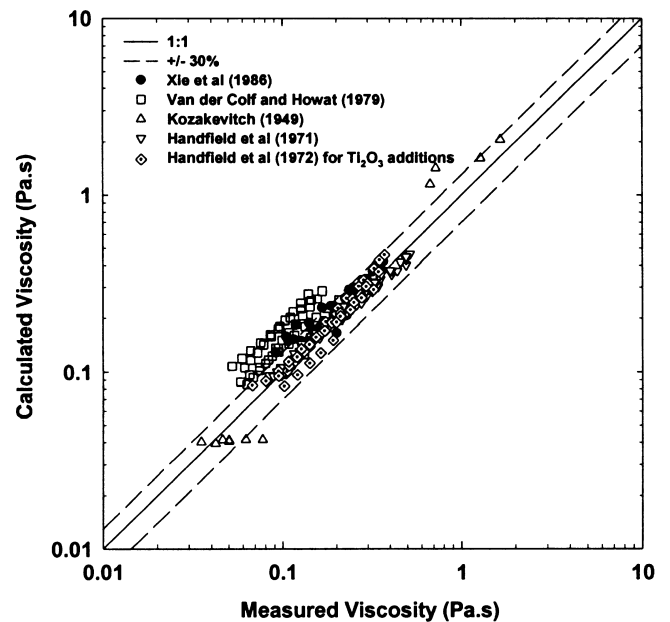


Figure 8. Comparison between the calculated viscosity and the experimental data<sup>4–8</sup> blast furnace type slags

This figure shows that the fit to most of the data is within 30% uncertainty except the data by Van der Colf and Howat<sup>5</sup>. As mentioned earlier, their data were consistently lower than those by Xie *et al.*<sup>4</sup> for slags with similar compositions. In order to examine the accuracy of the model for different variables, the calculated viscosity are compared with the data by Xie *et al.*<sup>4</sup> and Handfield *et al.*<sup>6-7</sup> directly with respect to variations in temperature and TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> additions. It should be mentioned that the model predicts continuous reduction of viscosity with addition of Ti<sub>2</sub>O<sub>3</sub> as shown in Figure 7. However, Handfield *et al.*'s data<sup>7</sup> showed that 15% Ti<sub>2</sub>O<sub>3</sub> addition caused viscosity to decrease more so than for 20% Ti<sub>2</sub>O<sub>3</sub>. Further investigations may be required to clarify the behaviour in this region. The results shown in Figures 4 to 6 demonstrated the close fit to the data. Furthermore the model provides correct representation of changes in viscosity with variations in temperature and slag chemistry.

### Structural role/behaviour of TiO<sub>x</sub>

The above review of experimental and modelling studies has shown that in general, additions of TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> to silicate melts will result in decreased viscosity. It is thus reasonable to consider that TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> predominantly act as network modifiers. There have been numerous studies on the structural role of titanium in melts and glasses, and the literature does show inconsistencies in findings. Mysen<sup>26</sup> reviewed the spectroscopic data on titania bearing glasses and noted the findings from various spectroscopic measurements tended to indicate that more than one structural position of Ti<sup>4+</sup> might be possible.

It has been also proposed<sup>27</sup> that, since the Ti<sup>4+</sup> cation is larger than the Si<sup>4+</sup> cation, then Ti-O-Ti and Ti-O-Al bonds are expected to be weaker than Si-O-Si and Si-O-Al bonds; thus addition of TiO<sub>2</sub> to highly polymerized aluminosilicate melts will decrease their viscosity. In the case of non-silicate TiO<sub>2</sub> containing slags, i.e., high titania slags, the viscosity measurements on the CaO(30 wt%)-TiO<sub>2</sub>(70%) binary melt and Soreslag (FeO-TiO<sub>2</sub> rich slags) by Handfield and Charrette<sup>28</sup> have shown that when the slags are completely molten, viscosity was as low as 0.03 Pa.s. Furthermore, the viscosity value is independent of temperature and the variation of FeO from 3.3 to 15 wt% did not seem to influence the viscosity of the Soreslag. The effect of TiO<sub>2</sub> on viscosity of slags as discussed suggests that TiO<sub>2</sub> acts in a similar way to other metal oxides, such as CaO or FeO. The possible variation to the coordination, namely, tetrahedral, when TiO<sub>2</sub> is low in silicate melts<sup>26</sup>, or octahedra, in TiO<sub>2</sub> rich slags, does not seem to alter the bonding characteristic of TiO<sub>2</sub>. The strength of the Ti-O bonds seems to be much weaker than that of the Si-O or Al-O bonds in the melts.

### Conclusions

The review of the published viscosity data for TiO<sub>x</sub> containing silicate melts showed that the addition of TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> resulted in a decrease in viscosity. The CSIRO's viscosity model was extended to TiO<sub>x</sub> containing silicate melts by treating TiO<sub>2</sub> and Ti<sub>2</sub>O<sub>3</sub> as network modifiers. Good agreement between the predicted and measured viscosity of ternary systems was obtained. The predictive power of the model has been demonstrated by a good fit to the measured viscosity of the blast furnace type slags. The model was able to represent effects of temperature and variations in slag compositions with respect to each component accurately.

### Acknowledgements

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